

POLI666: Lab #1

Olivier Bergeron-Bouutin

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Moving from predictive to causal inference

Do we care about bias?

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- Is a biased estimate necessarily a sign of a useless model? Under what circumstances would you care if an estimate is biased, and under what circumstances would you not?

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- ...Any examples?

Consider the following linear model from Gerber, Green and Larimer (2008):

$$\text{Turnout}_i = \beta_0 + \beta_1 \text{CivicDuty}_i + \beta_2 \text{Hawthorne}_i + \beta_3 \text{Self}_i + \beta_4 \text{Neighbors}_i + \epsilon_i \quad (1)$$

Model 1	
(Intercept)	0.297 [0.295, 0.299]
civicduty	0.018 [0.013, 0.023]
hawthorne	0.026 [0.021, 0.031]
self	0.049 [0.043, 0.054]
neighbors	0.081 [0.076, 0.086]
Num.Obs.	344084
R2	0.003
R2 Adj.	0.003

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- Conversely, I can have a model riddled with biased coefficients but with high predictive power

Some food for thought

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Cool causal inference work that can get you thinking:

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Acharya, Blackwell and Sen 2016 (IV)

- Cotton suitability as an instrument for % of Southern counties' population that is black before the abolition of slavery.

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- Does the treatment effect identified in my sample generalize?

Effect size in Gerber et al. 2008

Rolling ATE as we draw random observations from the Gerber et al. sample:



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- Hannity vs Carlson paper: “a one standard deviation increase in relative viewership of *Hannity* relative to *Tucker Carlson Tonight* is associated with approximately 34 percent more COVID-19 cases on March 14 and approximately 24 percent more COVID-19 deaths on March 28.”

Notation and terminology

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Estimate

The numerical value taken on by an estimator for a particular sample of data.

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4. Under repeated sampling, estimates have a distribution, which we call a sampling distribution.
5. Estimators have different properties.

Potential outcomes framework

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Realized outcome

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Will I ever observe this quantity? **NO!** That's the fundamental problem of causal inference

- And why we need to learn all of this complicated stuff in the first place...

Fundamental problem of causal inference:

Only one of the potential outcomes is realized:

$$Y_i = D_i Y_i(1) + (1 - D_i) Y_i(0) = \begin{cases} Y_i(1), & \text{if } D_i = 1 \\ Y_i(0), & \text{if } D_i = 0 \end{cases} \quad (3)$$

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- Causal inference as a problem of missing data

Ideal data

Without the fundamental problem of causal inference, this is what our data would look like:

D_i	$Y_i(1)$	$Y_i(0)$	Y_i
1	2	1	?
1	3	3	?
0	5	4	?
1	3	1	?
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I can compute τ_i since for each unit i , I have access to both potential outcomes

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- Namely: $\tau_i = \tau \forall i$

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But, again, we cannot actually compute $\mathbb{E}[\tau_i]$ because we never observe τ_i

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- We have “missing data” that prevents us from observing τ_i , and therefore τ
- We have to use the observed (incomplete) data to *infer* the estimand

The role of randomization

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No: I still can't observe the potential outcomes.

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- *No_HH*: Number of households
- *MAIN_AL_P*: Mean agricultural laborers
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Balance checks in R

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We want to show the control and treatment groups are not systematically different. There are many ways of going about this! Ideas?