POLI666: Lab #1

Olivier Bergeron-Bouutin January 19th, 2021

Moving from predictive to causal

inference

Remember this question from 618's 5th problem set?

 Is a biased estimate necessarily a sign of a useless model? Under what circumstances would you care if an estimate is biased, and under what circumstances would you not?

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- As long as our models could produce predictions that satisfied whichever inferential goal we had
- · ...Any examples?

Consider the following linear model from Gerber, Green and Larimer (2008):

$$Turnout_i = \beta_0 + \beta_1 CivicDuty_i + \beta_2 Hawthorne_i + \beta_3 Self_i + \beta_4 Neighbors_i + \epsilon_i$$
 (1)

	Model 1
(Intercept)	0.297 [0.295, 0.299]
civicduty	0.018 [0.013, 0.023]
hawthorne	0.026 [0.021, 0.031]
self	0.049 [0.043, 0.054]
neighbors	0.081 [0.076, 0.086]
Num.Obs.	344084
R2	0.003
R2 Adj.	0.003

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- Conversely, I can have a model riddled with biased coefficients but with high predictive power



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 How do we differentiate the effect of economic conditions from the effect of media coverage of the economy? Crossing an unemployment "milestone" (i.e. crossing a round number) is quasi-random and produces an exogenous change in media coverage.

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 Use data data from the 99 state legislatures on legislators' committee assignments; assignment to legislative committees causes an increase in campaign donations from relevant interest groups.

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Acharya, Blackwell and Sen 2016 (IV)

• Cotton suitability as an instrument for % of Southern counties' population that is black before the abolition of slavery.

Causal inference is hard! We must keep in mind several questions/elements:

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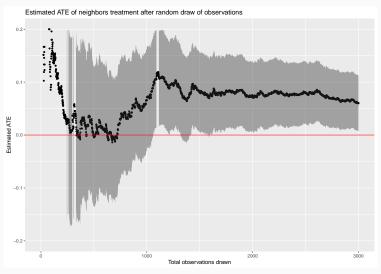
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- · Do I have the statistical power to detect anticipated au?
- Does the treatment effect identified in my sample generalize?

Effect size in Gerber et al. 2008

Rolling ATE as we draw random observations from the Gerber et al. sample:



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 John Stewart paper in Electoral Studies: the claim that John Stewart leaving The Daily Show increased county-level vote for Trump by 1.1% just does not sound right! (paper was retracted due to a coding error)

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- John Stewart paper in Electoral Studies: the claim that John Stewart leaving The Daily Show increased county-level vote for Trump by 1.1% just does not sound right! (paper was retracted due to a coding error)
- Hannity vs Carlson paper: "a one standard deviation increase in relative viewership of Hannity relative to Tucker Carlson Tonight is associated with approximately 34 percent more COVID-19 cases on March 14 and approximately 24 percent more COVID-19 deaths on March 28."

Notation and terminology

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Estimate

The numerical value taken on by an estimator for a particular sample of data.

Some things to keep in mind:

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- 5. Estimators have different properties.

Potential outcomes framework

For each unit i, we imagine two states of the world: under treatment and under control

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Realized outcome

$$Y_i(d) = \begin{cases} Y_i(1), & \text{Potential outcome for unit } i \text{ under treatment} \\ Y_i(0), & \text{Potential outcome for unit } i \text{ under control} \end{cases} \tag{2}$$

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Will I ever observe this quantity? **NO!** That's the fundamental problem of causal inference

 And why we need to learn all of this complicated stuff in the first place...

Only one of the potential outcomes is realized:

$$Y_i = D_i Y_i(1) + (1 - D_i) Y_i(0) = \begin{cases} Y_i(1), & \text{if } D_i = 1 \\ Y_i(0), & \text{if } D_i = 0 \end{cases} \tag{3}$$

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- · Causal inference as a problem of missing data

Without the fundamental problem of causal inference, this is what our data would look like:

$\overline{D_i}$	$Y_i(1)$	$Y_i(0)$	Y_i
1	2	1	?
1	3	3	?
0	5	4	?
1	3	1	?
0	2	4	?

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I can compute τ_i since for each unit i, I have access to both potential outcomes

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- · Namely: $\tau_i = \tau \ \forall i$

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But, again, we cannot actually compute $\mathbb{E}[au_i]$ because we never observe au_i

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- · We have to use the observed (incomplete) data to infer the estimand

The role of randomization

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Is this something we can empirically test?

No: I still can't observe the potential outcomes.

Balance checks in R

We'll use Dunning and Nilekani (2013), who investigate the effect of ethnic quotas on redistribution in India. The unit of analysis is the village council.

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We want to show the control and treatment groups are not systematically different. There are many ways of going about this! Ideas?